



# A New View of Intra-Regular $\mathcal{AG}$ -Groupoids in Terms of Generalized Cubic Ideals

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## Abstract

In this paper we characterize the intra-regular  $\mathcal{AG}$ -groupoids in terms of generalized cubic set. We show that the concept of  $(\in_{\Gamma}, \in_{\Gamma} \vee q\Delta)$ -cubic ideals and of  $(\in_{\Gamma}, \in_{\Gamma} \vee q\Delta)$ -cubic interior ideals in an intra-regular  $\mathcal{AG}$ -groupoid  $S$  with left identity coincides. We additionally demonstrate that an  $\mathcal{AG}$ -groupoid  $S$  with left identity is intra-regular if and only if  $\beta_1 \wedge^* \beta_2 = \beta_1 \circ^* \beta_2$  for all  $(\in_{\Gamma}, \in_{\Gamma} \vee q\Delta)$ -cubic quasi ideals  $\beta_1 = \langle \tilde{\mathfrak{S}}_{\beta_1}, \mathfrak{h}_{\beta_1} \rangle$  and  $\beta_2 = \langle \tilde{\mathfrak{S}}_{\beta_2}, \mathfrak{h}_{\beta_2} \rangle$  of  $S$ .

**Keywords:**  $\mathcal{AG}$ -groupoids; intra-regular  $\mathcal{AG}$ -groupoids; cubic sets, generalized sub  $\mathcal{AG}$ -groupoids; generalized cubic ideals.